

Package ‘fdaPOIFD’

September 2, 2025

Type Package

Title Partially Observed Integrated Functional Depth

Version 2.0.1

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Description Integrated Functional Depth for Partially Observed Functional Data and applications to visualization, outlier detection and classification. It implements the methods proposed in: Elías, A., Jiménez, R., Paganoni, A. M. and Sangalli, L. M., (2023), ``Integrated Depth for Partially Observed Functional Data", Journal of Computational and Graphical Statistics, <doi:10.1080/10618600.2022.2070171>. Elías, A., Jiménez, R., & Shang, H. L. (2023), ``Depth-based reconstruction method for incomplete functional data", Computational Statistics, <doi:10.1007/s00180-022-01282-9>. Elías, A., Nagy, S. (2024), ``Statistical properties of partially observed integrated functional depths", TEST, <doi:10.1007/s11749-024-00954-6>.

License GPL-3

Encoding UTF-8

LazyData true

RoxygenNote 7.3.2

Depends R (>= 3.5.0)

Suggests knitr, rmarkdown

VignetteBuilder knitr

Imports stats, ggplot2, tibble, magrittr, reshape2, patchwork, igraph

URL <https://github.com/ae fdz/fdaPOIFD>

BugReports <https://github.com/ae fdz/fdaPOIFD/issues>

NeedsCompilation no

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Repository CRAN
Date/Publication 2025-09-02 21:00:02 UTC

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boxplotPOFD	<i>Functional Boxplot for Partially Observed Functional Data</i>
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Description

Plots the Functional Boxplot for PoFD and returns the magnitude and domain outliers. Magnitude outliers in blue, a dotted red indicates that the outlier situation occurs in a region with less than fdom proportion of the central region.

Usage

```
boxplotPOFD(  
  data,  
  depth,  
  centralRegion = 0.5,  
  fmag = 1.5,  
  fdom = 0,  
  plot = TRUE  
)
```

Arguments

data	matrix p by n, being n the number of functions and p the number of grid points.
depth	depth used to build the functional boxplot. Default is MBD, see POIFD function for other definitions.
centralRegion	number between 0 and 1 determining the proportion of the deepest functions that builds the central region.

fmag	factor to enhance the functional central region and determine the functional whiskers. Default is equal to 1.5. The whiskers provide the rule to unmask magnitude outliers.
fdom	factor that provides the maximum proportion of observed functions in the central region to consider a magnitude outlier as a domain outlier also. A value equals to 0 means that domain outliers are those functions that are observed on the domain where any of the functions building the central region are observed. A value equals to 1 determine as domain outlier any magnitude outlier out of the region where the central region is completely observed.
plot	if the plot is shown or not.

Value

a list with the functional boxplot for PoDF the magnitude outliers and the domain outliers.

References

Sun, Y. and Genton, M. G. (2011). Functional boxplots. *Journal of Computational & Graphical Statistics*, 20(2):316–334.

Examples

```
boxplotPOFD(exampleData$PoFDextremes_outliers,
depth = "MBD",
centralRegion = 0.5,
fmag = 1.5, fdom = 0)
```

commondomainPOFD	<i>Common Domain Observability</i>
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Description

Generates samples of functions observed in a common domain in the center part of the domain. See Elías et al (2020).

Usage

```
commondomainPOFD(data, observability = NULL, pIncomplete = NULL)
```

Arguments

data	functional data completely observed. pxn matrix being n the number of curves and p the number of evaluation points.
observability	mean observed proportion of the domain where each function is observed.
pIncomplete	number between 0 and 1 related to the proportion of curves that suffers partially observability. The default is 1 meaning that all the sample curves are partially observed.

Value

a list containing two elements 1) a functional sample and 2) the same sample of functions but partially observed following one of the schemes described in the argument type.

References

Elías, Antonio, Jiménez, Raúl, Paganoni, Anna M. and Sangalli, Laura M. (2020). Integrated Depths for Partially Observed Functional Data.

Examples

```
data <- sapply(1:100, function(x) runif(1)*sin(seq(0, 2*pi, length.out = 200)) +
  runif(1)*cos(seq(0, 2*pi, length.out = 200)))

data_pofd <- commondomainPOFD(data, observability = 0.5, pIncomplete = 1)
```

depthbasedreconstructionPOFD

Depth-based reconstruction of partially observed functional data

Description

This function implements the reconstruction procedure [1] which is based on the depth measure [2] for partially observed functional data. Missing trajectories are imputed by the mean of the k nearest neighbors within the envelope. The parameter k is tuned minimizing the Mean Squared Error of the reconstruction in the observed part of the curve.

Usage

```
depthbasedreconstructionPOFD(data, id_recons = 1:dim(data)[2])
```

Arguments

data	Data matrix ‘p’ by ‘n’, being ‘n’ the number of functions and ‘p’ the number of grid points. The row names of the matrix should be the common evaluation grid and the column names the identifiers of each functional data.
id_recons	Vector indicating functions to be reconstructed. By default, all functions are reconstructed.

Details

[1] Elías, A., Jiménez, R., & Shang, H. L. (2023). Depth-based reconstruction method for incomplete functional data. *Computational Statistics*, 38(3), 1507-1535.

[2] Elías, A., Jiménez, R., Paganoni, A. M., & Sangalli, L. M. (2023). Integrated depths for partially observed functional data. *Journal of Computational and Graphical Statistics*, 32(2), 341-352.

Value

The reconstructed data matrix 'recons_data'.

Examples

```
data <- exampleData$PoFDintervals
recons_data <- depthbasedreconstructionPOFD(data, id_recons = 1:2)
```

envelope	<i>Envelope algorithm</i>
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Description

Code for obtaining the envelope J_i of a curve specified by the index i . The implementation is based on Algorithm 1 in [1]. References:

Usage

```
envelope(data, i, max_iter = 10)
```

Arguments

- data Data matrix.
- i Index of curve.
- max_iter Maximum number of nearest curves considered in for loop. By default, max_iter = 5.

Details

[1] Elías, A., Jiménez, R., & Shang, H. L. (2023). Depth-based reconstruction method for incomplete functional data. Computational Statistics, 38(3), 1507-1535.

Value

Envelope (set of indices).

exampleData

exampleData

Description

An illustrative Functional Gaussian processes with different partially observed patterns with outliers and without outliers.

Usage

```
exampleData
```

Format

A list with three data sets (functions by columns):

PoFDintervals Partially observed functional data in intervals

PoFDextremes Partially Observed functional data with missing intervals at the extremes

PoFDextremes_outliers Same as above but including two magnitude and shape outliers

PoFDintervals_list Partially observed data without a common domain. Each function is one element of the list, containing the evaluation points (x) and the evaluated function (y).

References

Elías, Antonio, Jiménez, Raúl, Paganoni, Anna M. and Sangalli, Laura M. (2020). Integrated Depths for Partially Observed Functional Data.

Examples

```
data(exampleData)
plotPOFD(exampleData$PoFDintervals)
```

intervalPOFD

Random Interval Observability

Description

Generates samples of functions observed in different intervals. See Elías et al (2020).

Usage

```
intervalPOFD(data, observability = NULL, ninterval = NULL, pIncomplete = NULL)
```

Arguments

data	functional data completely observed. pxn matrix being n the number of curves and p the number of evaluation points.
observability	mean observed proportion of the domain where each function is observed.
ninterval	if type = "interval", n_interval is an integer with the number of observed intervals 1, 2, 3... Large values of this parameter requires a large parameter p to guarantee the observability level.
pIncomplete	number between 0 and 1 related to the proportion of curves that suffers partially observability. The default is 1 meaning that all the sample curves are partially observed.

Value

a list containing two elements 1) a functional sample and 2) the same sample of functions but partially observed following one of the schemes described in the argument type.

References

Elías, Antonio, Jiménez, Raúl, Paganoni, Anna M. and Sangalli, Laura M. (2020). Integrated Depths for Partially Observed Functional Data.

Examples

```
data <- sapply(1:100, function(x) runif(1)*sin(seq(0, 2*pi, length.out = 200)) +
runif(1)*cos(seq(0, 2*pi, length.out = 200)))

data_pofd <- intervalPOFD(data, observability = 0.5, ninterval = 2, pIncomplete = 1)
```

learningK

Learning k

Description

This function chooses an optimal parameter k (denoting the number of curves within the envelope that are considered for reconstruction).

Usage

```
learningK(data, i, J)
```

Arguments

data	Data matrix.
i	Index of curve.
J	Envelope.

Value

Optimal parameter k.

outliergramPOFD	<i>Outliergram for Partially Observed Functional Data</i>
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Description

Plots the Outliergram for PoFD and returns the shape outliers.

Usage

```
outliergramPOFD(data, fshape = 1.5, p1 = 1, p2 = 0, plot = TRUE)
```

Arguments

- | | |
|--------|---|
| data | matrix p by n, being n the number of functions and p the number of grid points. |
| fshape | inflation of the outliergram that determine the shape outlier rule. |
| p1 | parameter of the outliergram for resampling method. Default = 1. |
| p2 | parameter of the outliergram for resampling method. Default = 0. |
| plot | if the plot is shown or not. |

Value

a list with the functional outliergram for PoDF and the shape outliers.

References

Arribas-Gil, A. and Romo, J. (2014). Shape outlier detection and visualization for functional data: the outliergram. *Biostatistics*, 15(4):603–619.

Examples

```
outliergramPOFD(exampleData$PoFDextremes_outliers, fshape = 1.5, p1 = 1, p2 = 0)
```

plotPOFD

Plot Partially Observed Functional Data

Description

Plot the sample of partially observed curves and the proportion of observed functions.

Usage

```
plotPOFD(data)
```

Arguments

`data` matrix p by n , being n the number of functions and p the number of grid points.

Value

Plot of the partially observed functional data and the proportion of observed functions at each time point.

Examples

```
plotPOFD(exampleData$PoFDextremes)
```

POIFD

Integrated Depth for Partially Observed Functional Data

Description

Compute the depth measure of a partially observed functional data set proposed in [1]. If the functions are not observed in a common partially observed domain, the code first estimates the observation domain using the proposal in [2].

Usage

```
POIFD(data, type = c("HD", "FMD", "MBD", "MHRD"), phi, t = NULL)
```

Arguments

data	If functions are observed in a partially observed common grid 'data' is a matrix 'p' by 'n', being 'n' the number of functions and 'p' the number of grid points. The row names of the matrix should be the common evaluation grid and the column names the identifiers of each functional data. If functions do not have a common grid, 'data' must be a list of length 'n' where each element contains the values and evaluation points of each function. I.e. each list element must contain two vectors 'x', including the evaluation points, and 'y', the evaluated function values. For functions without a common grid, the function "POIFD") first apply the procedure to estimate the observation domain proposed in Elías, A., Nagy, S. (2025), TEST.
type	chosen depth measure. Halfspace depth ("HS"), Fraiman and Muniz depth ("FMD"), Modified band depth ("MBD") or Modified Half Region Depth and Modified Epi-graph/Hipograph Index "MHRD")
phi	phi function of weights for the POIFD. The default value is as in [1]: the proportion of observed functions at each time point.
t	If functions do not have a common grid, 't' represents the final common grid of evaluation points to apply the procedure to estimate the observation domain proposed in [2].

Details

[1] Elías, A., Jiménez, R., Paganoni, A. M., & Sangalli, L. M. (2023). Integrated depths for partially observed functional data. *Journal of Computational and Graphical Statistics*, 32(2), 341-352.

[2] Elías, A., Nagy, S. (2025). Statistical Properties of Partially Observed Integrated Funcional Depths. *TEST*, 34, 125-150.

Value

Ordered vector of depths. The names are the functions names (if provided) or the column position.

Examples

```
data <- exampleData$PoFDintervals
poifd <- POIFD(data, type = c("FMD"))

data <- exampleData$PoFDintervals_list
poifd <- POIFD(data, type = c("FMD"), t = seq(0, 1, length.out = 100))
```

sparsePOFD

Sparse Observability

Description

Generates samples of sparse functions. See Elías et al (2020).

Usage

```
sparsePOFD(data, observability = NULL, pIncomplete = NULL)
```

Arguments

<code>data</code>	functional data completely observed. pxn matrix being n the number of curves and p the number of evaluation points.
<code>observability</code>	observed proportion of the domain where each function is observed.
<code>pIncomplete</code>	number between 0 and 1 related to the proportion of curves that suffers partially observability. The default is 1 meaning that all the sample curves are partially observed.

Value

a list containing two elements 1) a functional sample and 2) the same sample of functions but partially observed following one of the schemes described in the argument type.

References

Elías, Antonio, Jiménez, Raúl, Paganoni, Anna M. and Sangalli, Laura M. (2020). Integrated Depths for Partially Observed Functional Data.

Examples

```
data <- sapply(1:100, function(x) runif(1)*sin(seq(0, 2*pi, length.out = 200)) +  
  runif(1)*cos(seq(0, 2*pi, length.out = 200)))  
  
data_pofd <- sparsePOFD(data, observability = 0.5, pIncomplete = 1)
```

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